

# To Solve Fuzzy Game Problem Using Pentagonal Fuzzy Numbers

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## ABSTRACT

In this paper, a new concept of Fuzzy game problem using Pentagonal fuzzy numbers with some operation is introduced. By using ranking to the payoffs, we convert the fuzzy valued game problem to crisp valued game problem, which can be solved using the row minima-column maxima. The solution of such fuzzy games with saddle point, by minimax-maximin principle is discussed.

**Keywords:** Fuzzy Number, Fuzzy Transportation Problem, Membership Function, Pentagonal Fuzzy Number, Ranking of Fuzzy Number.

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## I. INTRODUCTION

Game theory is a mathematical theory that deals with the general features of competitive situations like some operations of pentagonal fuzzy numbers in a formal abstract way. The focus in this paper is on the minimax principle which states that each competitor will act so as to minimize one player's maximum loss (or maximize one player's minimum gain), then the opponent still can take advantage for this knowledge to reduce the expected payoff to the first player. We have analyzed the solution of such fuzzy games with saddle point, by minimax – maximin principle.

## II. PRELIMINARIES

### 2.1. Fuzzy Set:

A fuzzy set is characterized by a membership function mapping elements of a domain, space, or universe of discourse  $X$  to the unit interval  $[0,1]$ . (i.e.)  $A = \{x, \mu_A(x); x \in X\}$  here  $\mu_A : X \rightarrow [0,1]$  is a mapping called the degree of **membership function** of the fuzzy set  $A$  and  $\mu_A(x)$  is called the

membership value of  $x$  in the fuzzy set  $A$ . These membership grades are often represented by real numbers ranging from  $[0,1]$ .

### 2.2. Fuzzy Numbers:

A fuzzy set  $A$  defined on the set of real numbers  $R$  is said to be a fuzzy number if its membership function  $\mu_A : R \rightarrow [0, 1]$  has the following characteristics.

- (i)  $A$  is normal. It means that there exists an  $x \in R$  such that  $\mu_A(x) = 1$ .
- (ii)  $A$  is convex. It means that for every  $x_1, x_2 \in R$ ,  
 $\mu_A(\lambda x_1 + (1 - \lambda) x_2) \geq \min\{\mu_A(x_1), \mu_A(x_2)\}$ ,  $\lambda \in [0,1]$
- (iii)  $\mu_A$  is upper semi-continuous.
- (iv)  $\text{Supp}(A)$  is bounded in  $R$ .

## III. PENTAGONAL FUZZY NUMBER

The Fuzzy Number  $P$  is a Pentagonal Fuzzy.  $A_P$  is a Pentagonal Fuzzy number denoted  $A_P(a, b, c, d, e; 1)$  and its membership function  $\mu_{A_P}(x)$  is given below:

$$\mu_{Ap}(X) = \begin{cases} \frac{(x-a)}{b-a}, & a \leq x \leq b \\ \frac{(x-b)}{c-b}, & b \leq x \leq c \\ 1, & x = c \\ \frac{(d-x)}{d-c}, & c \leq x \leq d \\ \frac{(e-x)}{e-d}, & d \leq x \leq e \\ 0, & \text{otherwise} \end{cases}$$

#### IV. SADDLE POINT

A saddle point of a payoff matrix is that position in the payoff matrix. Where maximum of row minima, co-inside with the minimum of the column maxima. The pay off at the saddle point is called the value of the game denoted by gamma. The saddle point need not be unique. We denote the maximin value of the game by gamma( $\chi$ ) and the minimax value of the game by  $\bar{\gamma}$ .

The game is said to be fair. If  $\chi = 0 = \bar{\gamma}$

The game is said to be strictly determinable. If  $\chi = \bar{\gamma}$

#### V. MATHEMATICAL FORMULATION OF A FUZZY GAME PROBLEM

Let Player A have m strategies  $A_1, A_2 \dots A_m$  and Player B have n strategies  $B_1, B_2, \dots, B_n$ . Here, it is assumed that each player has his choices from amongst the pure strategies. Also it is assumed that player A is always the gainer and player B is always the loser. That is, all payoff are assumed in terms of player A. Let  $a_{ij}$  be the payoff which player A gains from player B if player A chooses strategy  $A_i$  and player B chooses strategy  $B_j$ . Then the payoff matrix to player A

#### VI. PROCEDURE FOR SOLVING FUZZY GAME PROBLEM

We shall present a solution to fuzzy game problem involving strategies of the players using triangular fuzzy numbers.

**Step 1:** Check whether a saddle point exists in the problem. If it exists, the solution can be obtained directly. If the saddle point does not exist, go to the next step.

**Step 2:** Comparison of column strategies.

(a). If elements of Column A  $\leq$  elements of Column B, Column A strategy dominates over column B

strategy. Hence delete column B strategy from the pay off matrix.

(b). Compare each column strategy with all possible column strategies and delete inferior strategies as far as possible.

**Step 3:** Comparison of row strategies.

(a). If elements of Row A  $\geq$  elements of Row B, Row A strategy dominates over Row B strategy. Hence delete Row B strategy from the pay off matrix.

(b). Compare each row strategy with all possible row strategies and delete inferior strategies as far as possible.

(c). The Game may reduce to a single cell giving information about the value of the game and optimal strategies of players. If not go to step 4.

**Step 4:** Dominance need not to be based on the superiority of pure strategies only. A given strategy can be dominated if it is inferior to an average of two or more other pure strategies.

#### 6.1. Numerical Example

Consider the following fuzzy game problem

	B <sub>1</sub>	B <sub>2</sub>	B <sub>3</sub>	B <sub>4</sub>	B <sub>5</sub>
A <sub>1</sub>	(7,8,9,10,11)	(1,2,3,4,5)	(1,0,1,2,3)	(4,6,8,10,12)	(-4,-2,0,4,8)
A <sub>2</sub>	(4,5,6,7,8)	(1,3,5,7,9)	(0,2,4,6,8)	(4,5,6,7,8)	(5,6,7,8,9)
A <sub>3</sub>	(0,1,2,3,4)	(0,2,3,4,5)	(1,2,3,4,5)	(1,2,3,4,5)	(4,6,8,10,12)
A <sub>4</sub>	(4,6,8,10,12)	(4,5,6,7,8)	(2,0,2,4,6)	(0,1,2,3,4)	(-1,0,1,2,3)

#### Solution

Using ranking function

$$R(\tilde{A}) = \frac{P_1 + P_2 + P_3 + P_4 + P_5}{5}$$

$$R(7, 8, 9, 10, 11) = \frac{7+8+9+10+11}{5} = \frac{45}{5}$$

$$R(7, 8, 9, 10, 11) = 9$$

Similarly

$$R(1,2,3,4,5) = 3 \quad R(-1,0,1,2,3) = 1 \quad R(4,6,8,10,12) = 8$$

$$R(-4,-2,0,4,8) = 0$$

$$R(4,5,6,7,8) = 6 \quad R(1,3,5,7,9) = 5 \quad R(0,2,4,6,8) = 4$$

$$R(4,5,6,7,8) = 6 \quad R(5,6,7,8,9) = 7$$

$$R(0,1,2,3,4) = 2 \quad R(0,2,3,4,5) = 4 \quad R(1,2,3,4,5) = 3$$

$$R(1,2,3,4,5) = 3 \quad R(4,6,8,10,12) = 8$$

$$R(4,6,8,10,12) = 5, \quad R(4,5,6,7,8) = 6, \quad R(-2,0,2,4,6) = 2,$$

$$R(0,1,2,3,4) = 2, \quad R(-1,0,1,2,3) = 1$$

$$B_1 \quad B_2 \quad B_3 \quad B_4 \quad B_5 \quad \text{Row min}$$

Minimax

